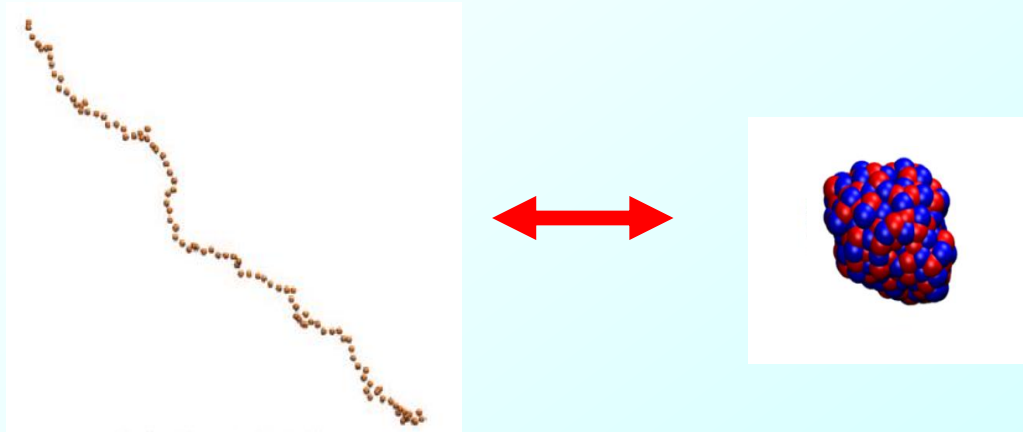


## *Nikolai Brilliantov*



***Controlled electrostatic collapse  
of polyelectrolytes***

## **In collaboration with:**

*Vladimir Palyulin (Skolkovo Institute of Science and Technology,  
Moscow, Russia)*

*Aleksei Gavrilov (Moscow State University, Moscow, Russia)*

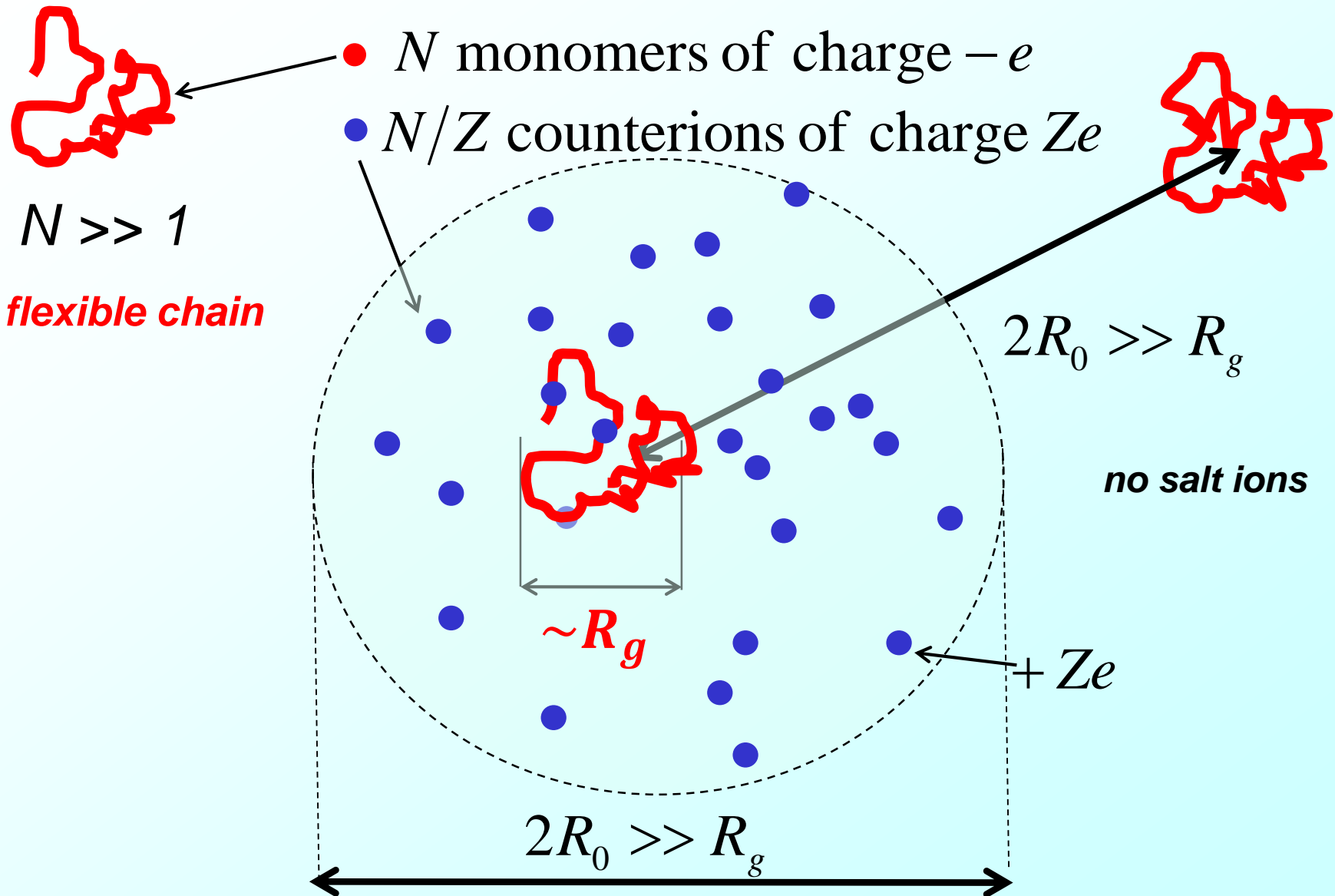
*Yury Budkov (Higher School of Economics, Moscow)*

## **Acknowledgement**

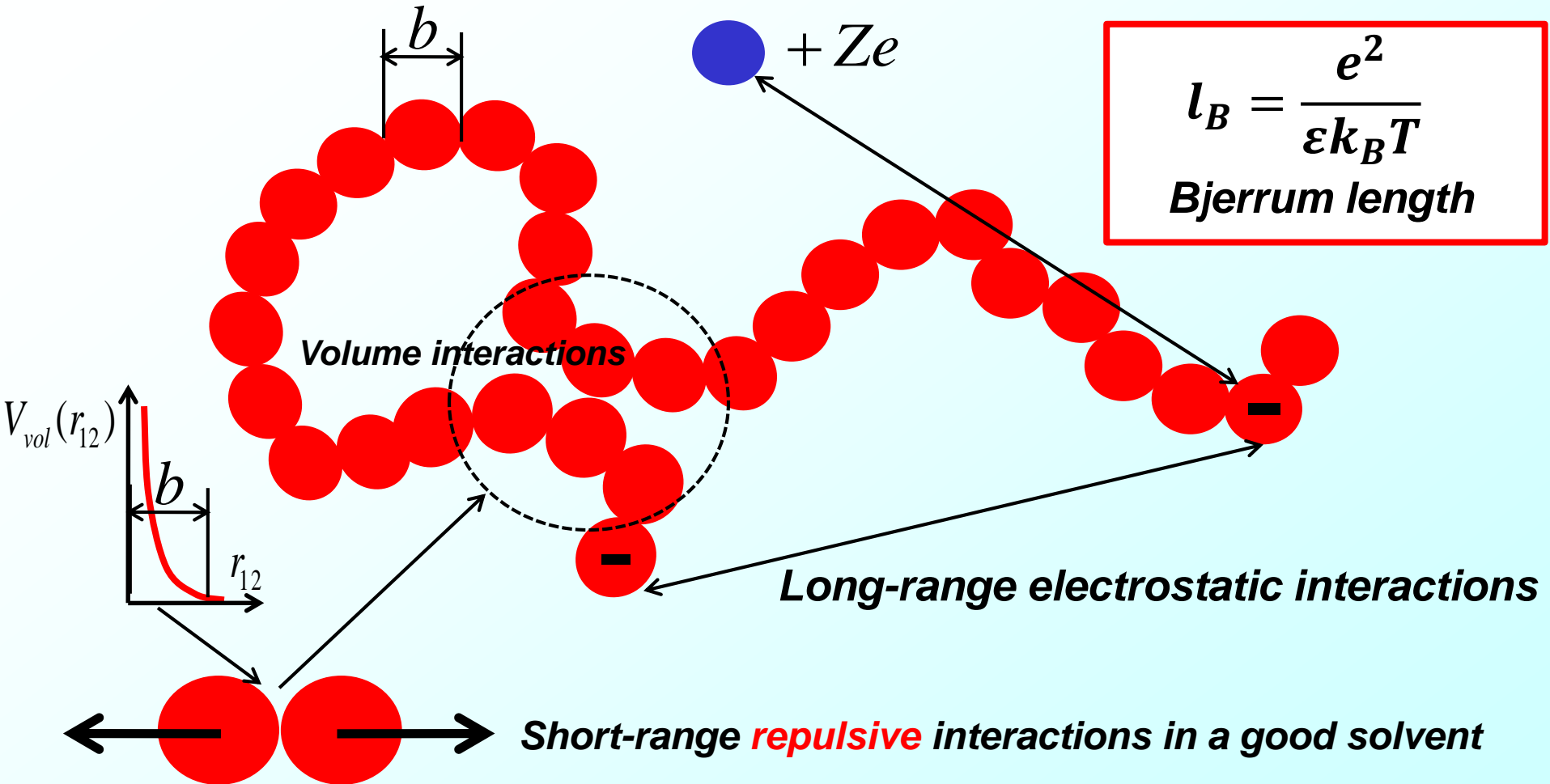
*Christian Seidel (Max Planck Institute of Colloidal and Interfaces,  
Potsdam, Germany)*

*Anvy Moly Tom, Satyavani Vemparala, and R. Rajesh  
(The Institute of Mathematical Sciences, Chennai, India)*

Consider a **dilute, salt free** solution of charged polymer chains in a **good solvent**



# Molecular interactions in a good solvent



$$l_B = \frac{e^2}{\epsilon k_B T}$$

**Bjerrum length**

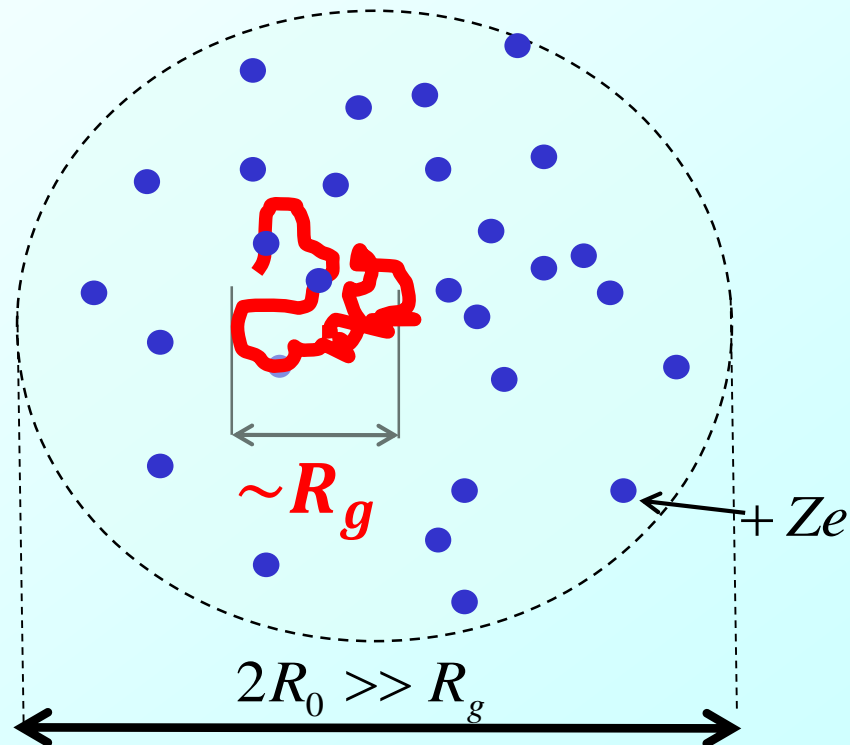
**Long-range electrostatic interactions**

$$V_{el}(r_{ij}) = \frac{q_i q_j}{\epsilon r_{ij}}$$

$\epsilon$  -dielectric permittivity

## The gyration radius $R_g$ may be controlled

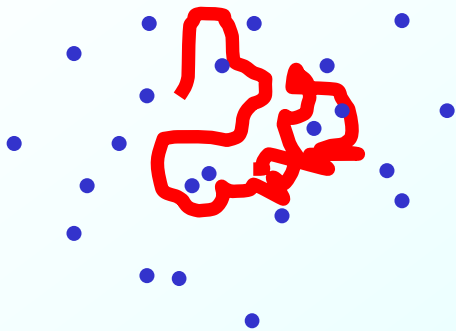
1. By properties of the solvent, reflected in the  $l_B$
2. By external electric field
3. By concentration of added salt



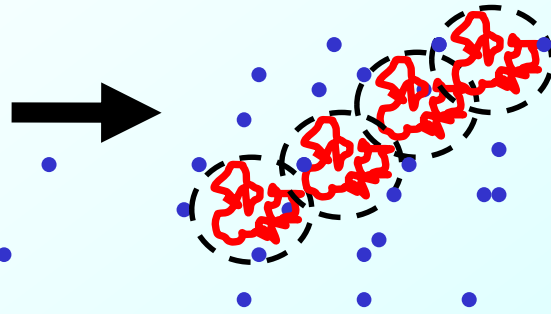
Consider variation of a chain conformation with increasing  $\ell_B$  that is, with increasing strength of electrostatic interactions?

$$\ell_B = \frac{l_B}{b}$$

very small  $\ell_B$

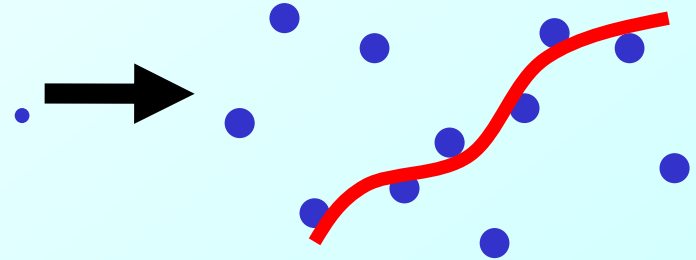


larger  $\ell_B$



formation of blobs

still larger  $\ell_B = 1$



Manning condensation

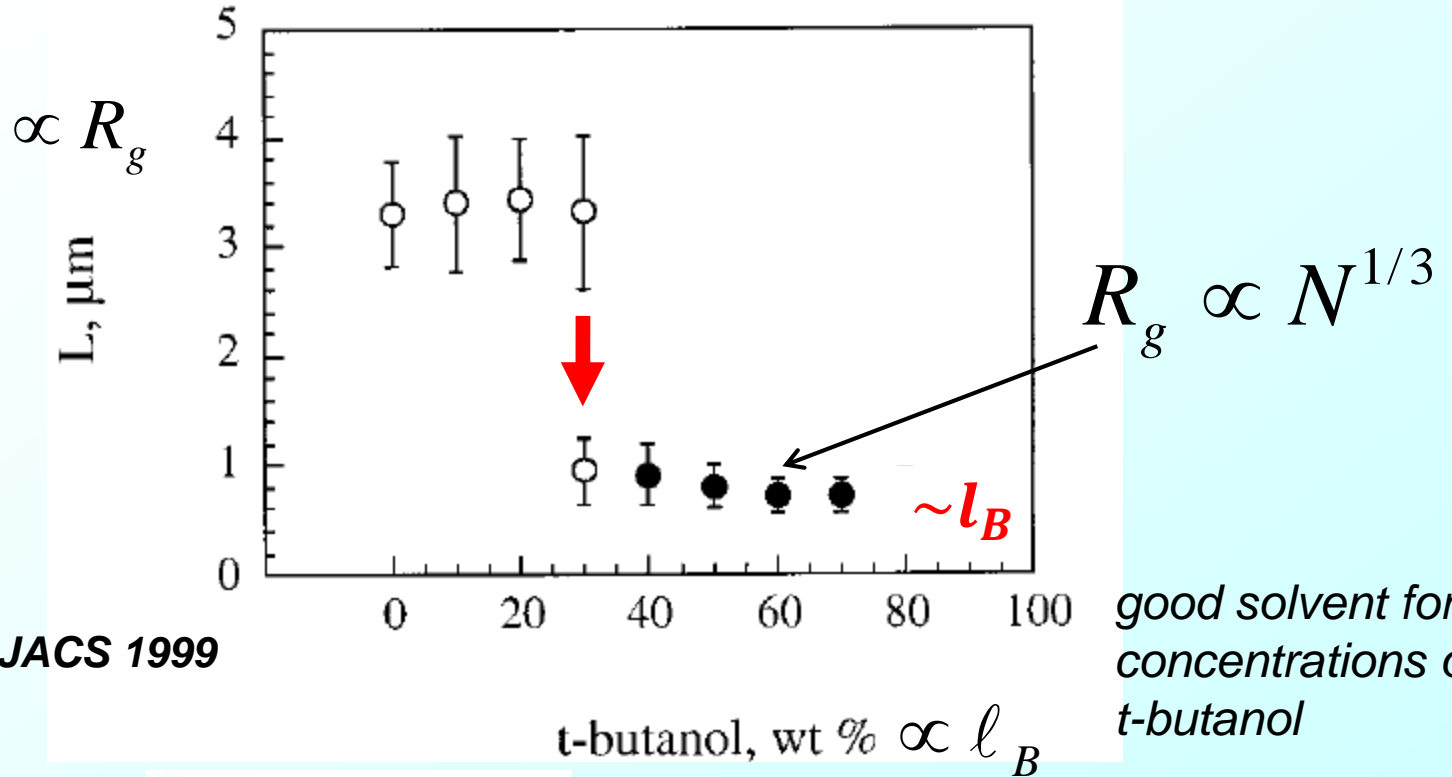
$$R_g \propto N^{3/5}$$

$$R_g \propto N$$

$$R_g \propto N$$

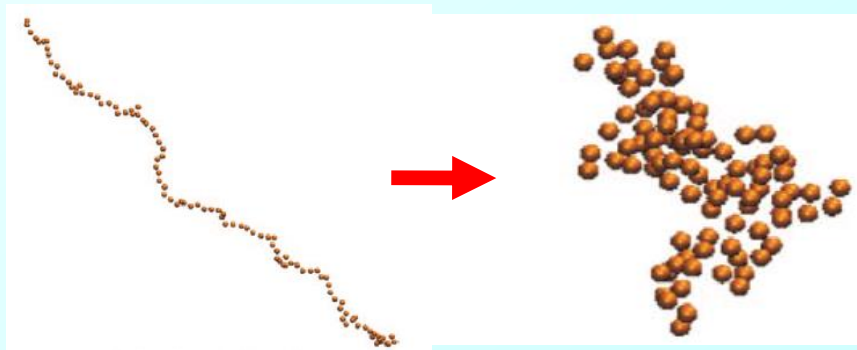
What happens next???

# Experiments show **collapse**:

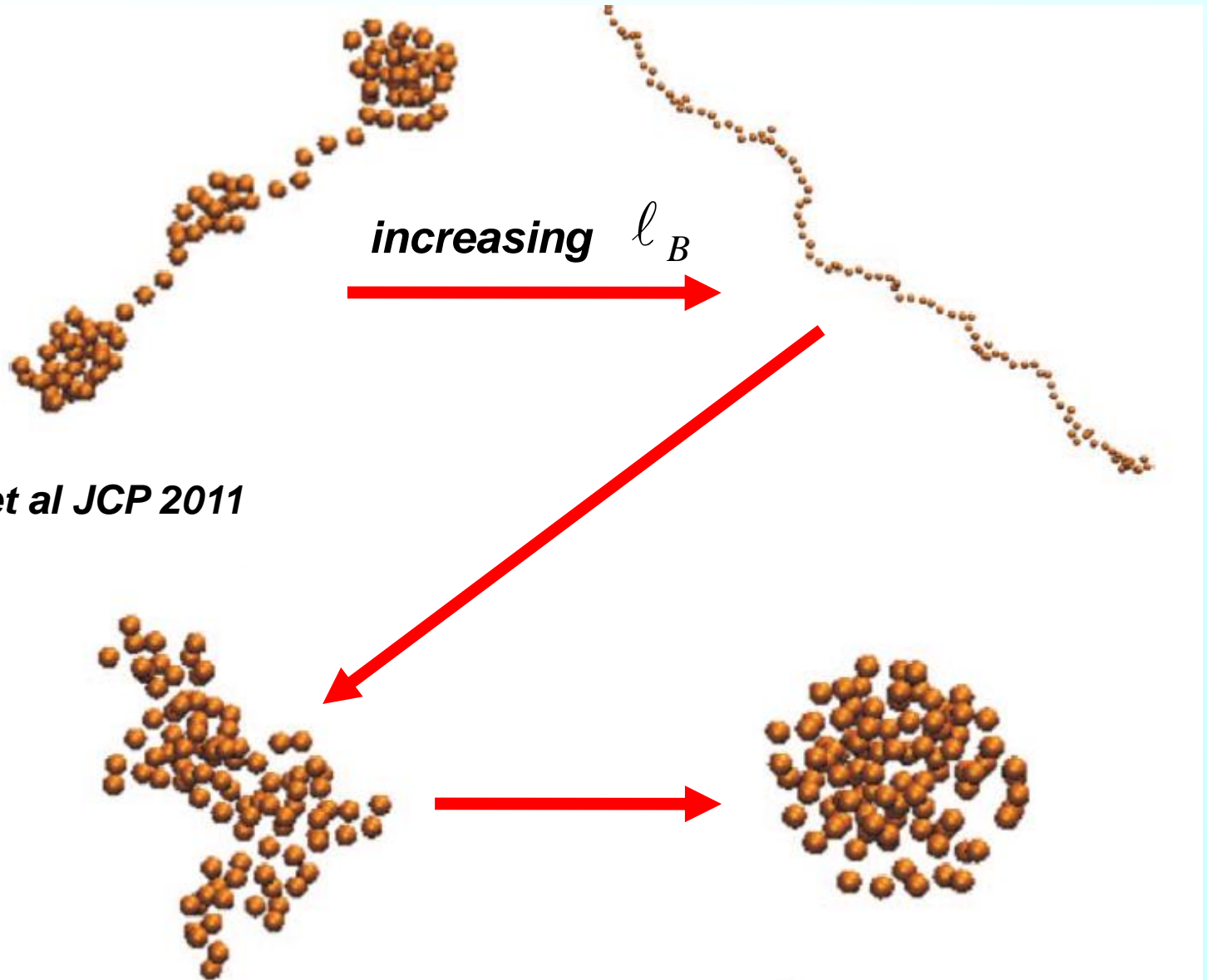


Melnikov, et al JACS 1999

good solvent for all concentrations of t-butanol



***MD shows collapse as well:***



***Varghese, et al JCP 2011***

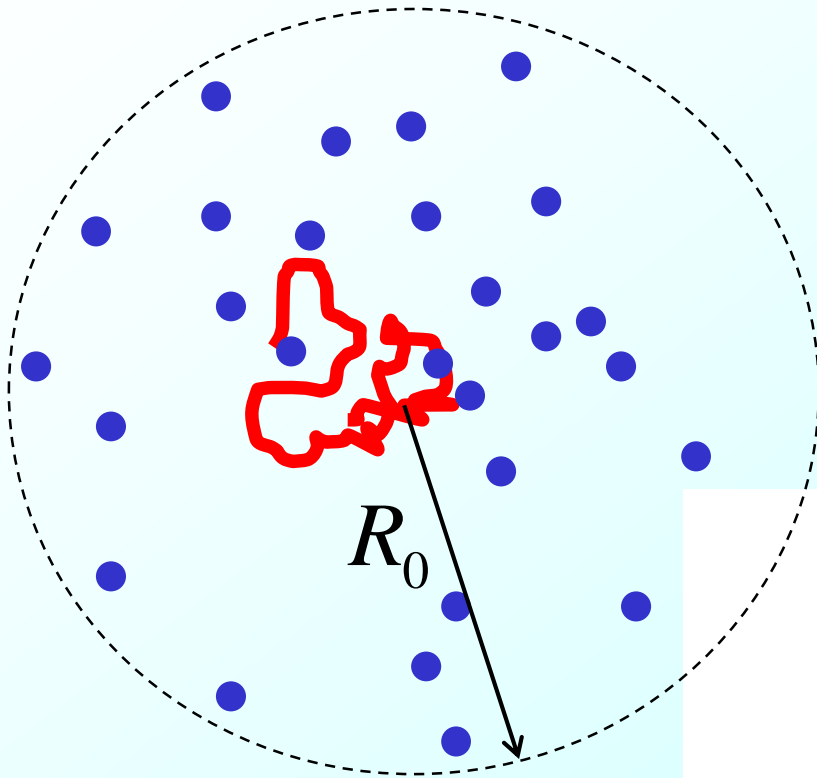


# The physical picture of the electrostatic collapse :

A key role play counterions:

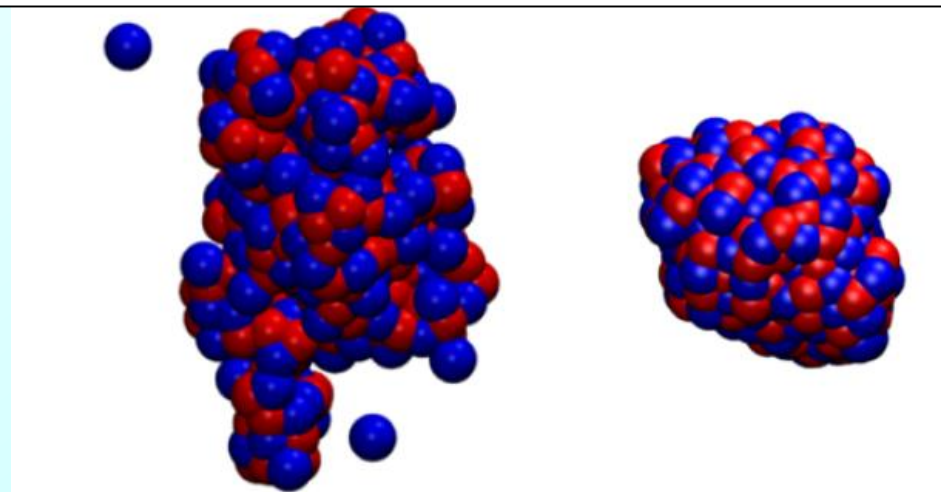
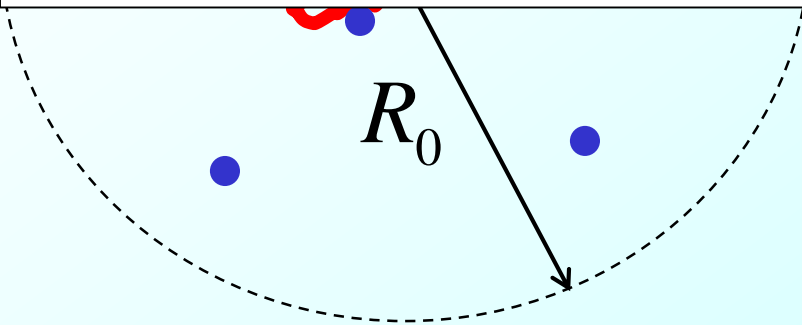
$$F = U - TS \text{ - free energy}$$

- If electrostatic interactions are **weak**, the **entropic term dominates** and the counterions are spread over the volume **without screening** of the monomers
- The monomers repulse and the chain has an **extended conformation**



***Physical picture of the electrostatic collapse :***

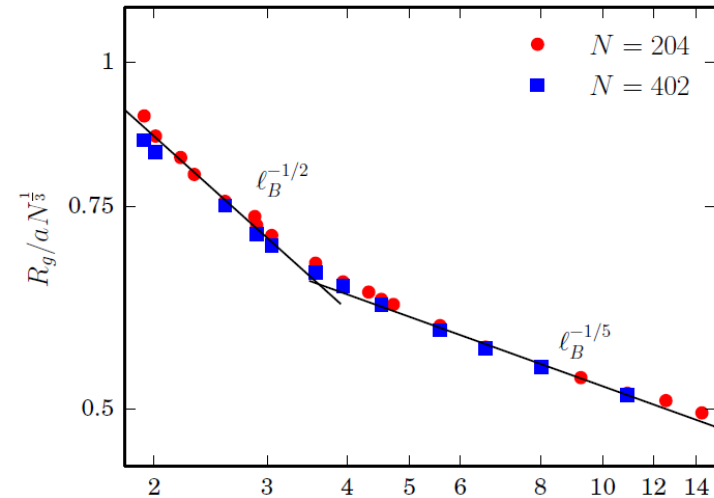
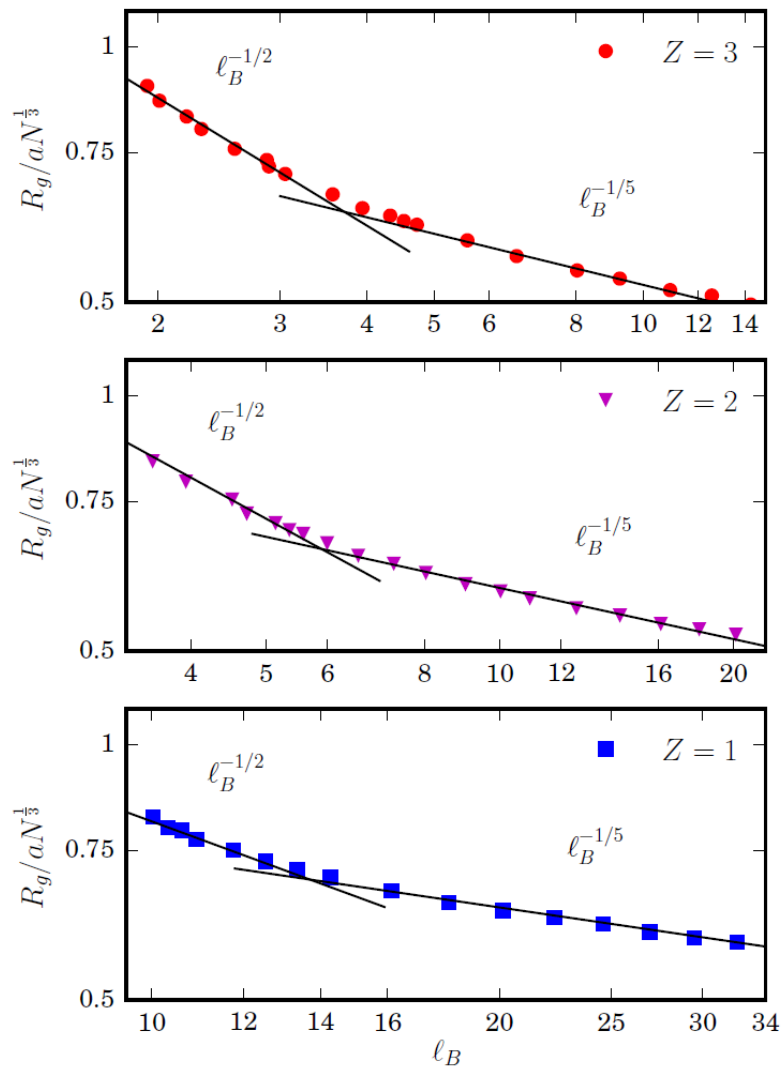
***But why an almost neutral chain is not in a loose coiled conformation?***



# MD study of the **electrostatic collapse**: Two collapse regimes

(Electrostatic and LJ interactions between particles)

A. M. Tom, S.Vemparala, R. Rajesh, & N. Brilliantov, *Phys. Rev. Lett.* 2016



●  $R_g \propto N^{1/3} \ell_B^{-1/2}$  --weak collapse

●  $R_g \propto N^{1/3} \ell_B^{-1/5}$  --strong collapse

These effects and dependences may NOT be explained by emerging dipole pairs, where

$$R_g \propto N^{1/3} \ell_B^{-2/3}$$

# Counterion fluctuation theory (CFT)

Free energy:

$$F(R_g) = \underbrace{F_{id.ch.}(R_g)}_{\text{ideal chain}} + \underbrace{F_{en.}(R_g)}_{\text{entropy of counterions}} + \underbrace{F_{el.}(R_g)}_{\text{electrostatic interactions}} + \underbrace{F_{vol.}(R_g)}_{\text{all volume interactions}}$$

We use the standard expressions for  $F_{id.ch.}$ ,  $F_{en.}$ ,  $F_{vol.}$ .

**Electrostatic interactions:**  $F_{el.mf} + F_{el.fluct}$   
 mean-field (with average charge)      fluctuations

$$\begin{aligned} \frac{F}{Nk_B T} &= \frac{9}{4N} (\alpha^2 + \alpha^{-2}) + \left( \frac{\widetilde{B}_2}{N^{1/2}\alpha} + \frac{\widetilde{B}_3}{\alpha^6} \right) + \frac{3}{Z} (1 - \tilde{\rho}) \ln(R_0/b) \\ &+ \frac{3\sqrt{6}l_B}{5\alpha} (1 - \tilde{\rho})(1 - 3R_g/R_0) + \frac{3}{2} \left( \frac{2}{\pi} \right)^{1/3} \frac{\sqrt{6}l_B Z^{2/3} \tilde{\rho}^{4/3}}{N^{1/6}\alpha} \end{aligned}$$

fraction of condensed counterions

$$\tilde{\rho} = \frac{N_{c.in}}{N_c}$$

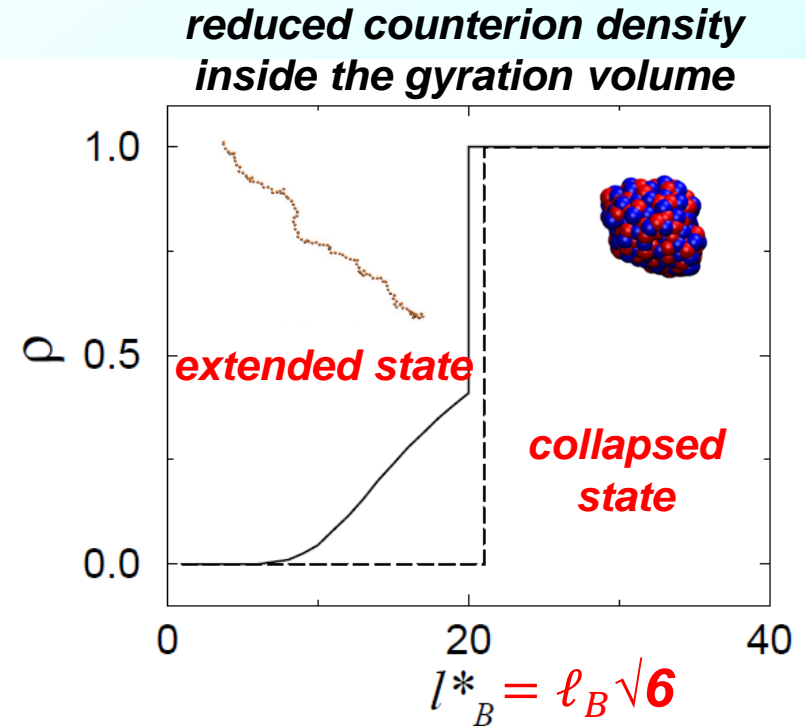
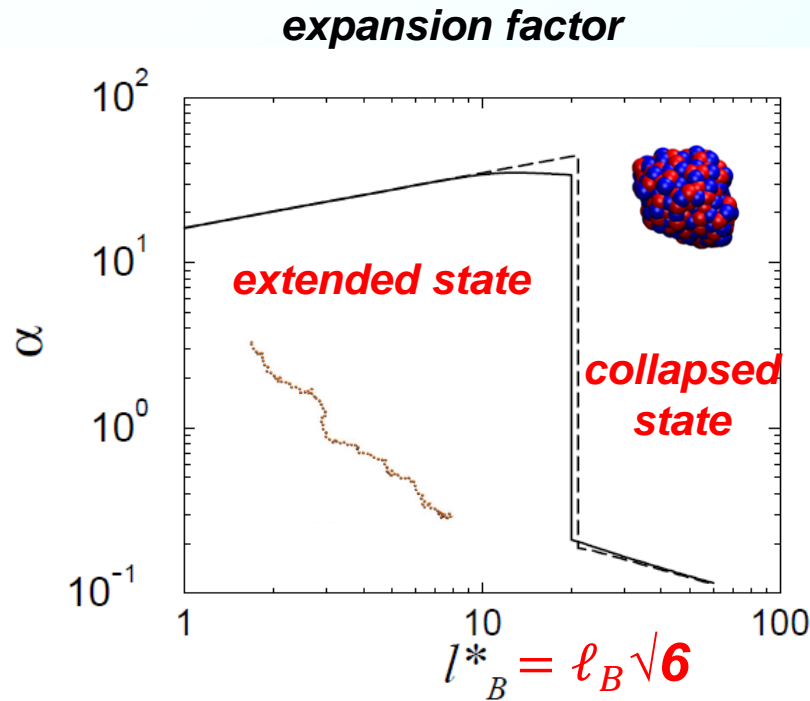
expansion factor

$$\alpha = \frac{R_g}{R_{g.id}} = \frac{6^{1/2} R_g}{N^{1/2} b}$$

**Minimizing**

$$F = F_{id.ch.} + F_{en.} + F_{el.} + F_{vol.}$$

**with respect to the gyration radius and counterion density, we obtain:**



**Brilliantov, Kuznetsov, Klein, Phys. Rev. Lett. 1998**

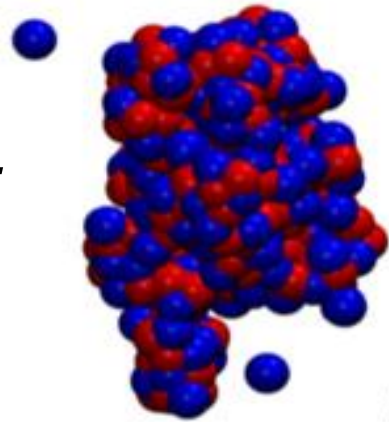
**The condition of a free motion of counterions within a globule, i.e. the validity of the CFT:**

$$\frac{E_{OCP}}{E_{dip}} = \frac{9c}{2} \frac{d_0}{a_c} = 1.77 \frac{\Gamma d_0}{l_B} = 5.02 \frac{d_0 Z^{5/3}}{b \alpha N^{1/6}} > 1$$

# **Collapse is accompanied by the condensation of the counterions inside the globule:**

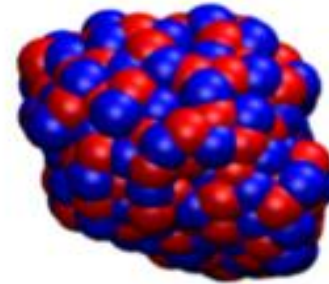
A. M. Tom, S.Vemparala, R. Rajesh, & N. Brilliantov Phys. Rev. Lett. 2016; Soft Matter 2017

*weak collapse --*

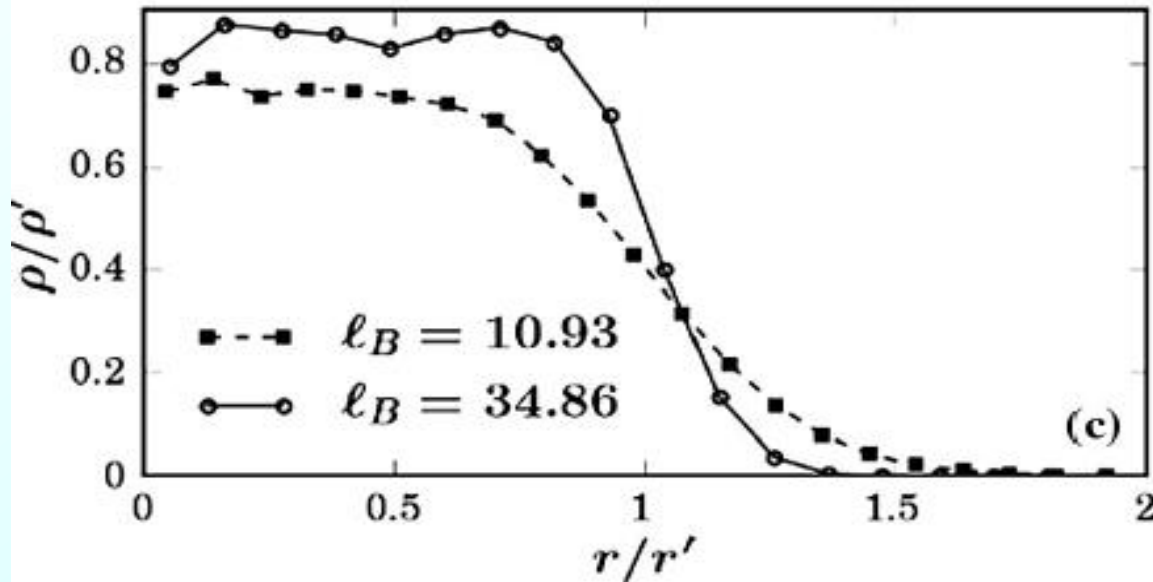


(a)

*--strong collapse*



(b)



# Counterion fluctuation theory

$$\alpha = \frac{R_g}{R_{g.id}} = \frac{6^{1/2} R_g}{N^{1/2} b}$$

Analytic estimates for different cases:

● Entropic term dominates:  $\ell_B N^{1/2} \ll \alpha R_0 / b \rightarrow \alpha \gg 1$

$$R_g \sim \ell_B^{1/3} N \quad \text{-- stretched chain}$$

● Counterion fluctuation term dominates:  $\ell_B N^{1/2} \gg \alpha R_0 / b \rightarrow \alpha \ll 1$

$$\alpha^3 > \tilde{B}_3 N^{-1/2} / \tilde{B}_2$$

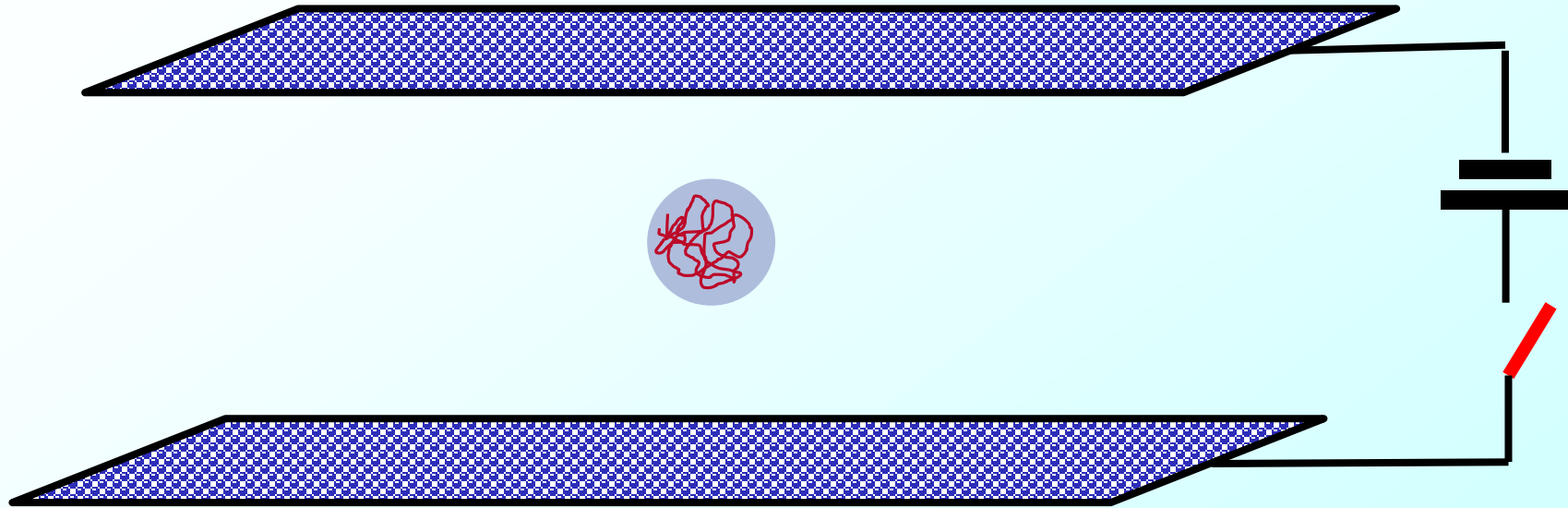
$$R_g \sim \ell_B^{-1/3} N^{1/3} \quad \text{-- weak collapse}$$

$$\alpha^3 < \tilde{B}_3 N^{-1/2} / \tilde{B}_2$$

$$R_g \sim \ell_B^{-1/5} N^{1/3} \quad \text{-- strong collapse}$$

# Field-regulated collapse

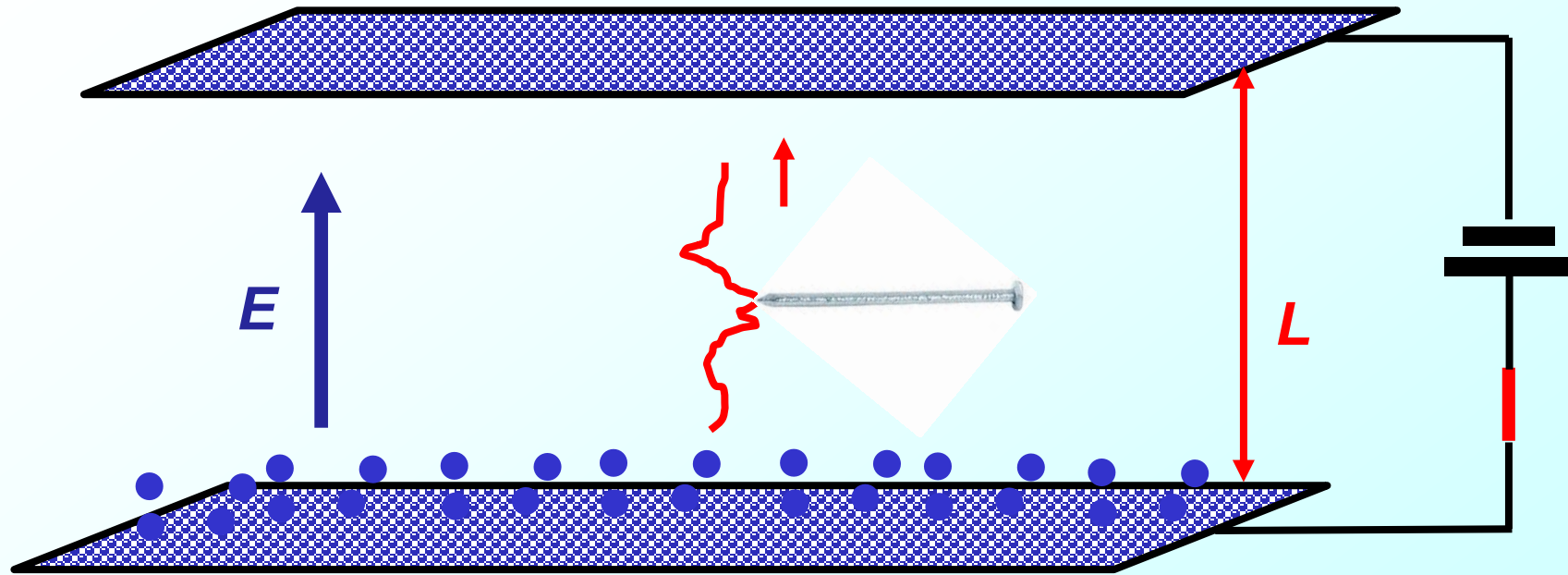
## Polyelectrolytes in **Electric** fields



- *Suppose that a PE chain in a good solvent has a globular conformation due to electrostatic collapse*
- *What happens if we **switch on** electrostatic field?*



**counterions will decondense and move towards low potential area, leaving the chain unscreened; the chain will expand**



**electrostatic interactions of chain and monomers**

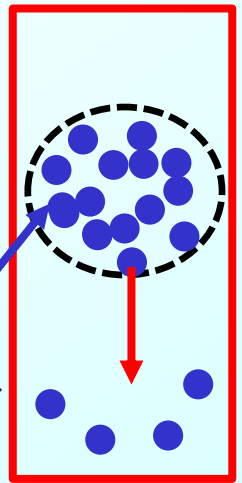
$$F(R_g) = \underbrace{F_{id.ch.}(R_g)}_{\text{ideal chain}} + \underbrace{F_{en.}(R_g)}_{\text{entropy of counterions}} + \underbrace{F_{el.}(R_g)}_{\text{all volume interactions}} + \underbrace{F_{vol.}(R_g)}_{\text{all volume interactions}} + \underbrace{F_E(R_g)}_{\text{electrostatic interactions of the chain and counterions with the field } E}$$

**electrostatic interactions of the chain and counterions with the field  $E$**

For the case  $eEL/k_B T \gg 1$

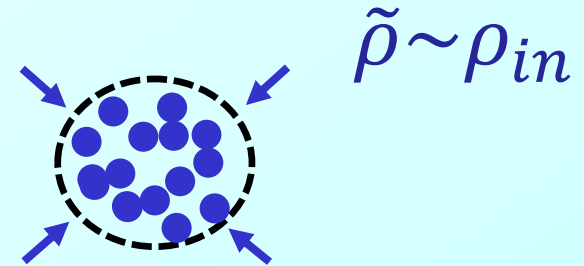
Two main **negative** terms compete:

$$\frac{F_{ch.E}}{Nk_B T} \sim - (1 - \tilde{\rho}) \frac{eEL}{k_B T} \quad \text{-- tries to decrease } \tilde{\rho} \sim \rho_{in}$$



and

counterion **fluctuation** term:  $\sim - \ell_B \tilde{\rho}^{\frac{4}{3}} / \alpha N^{1/6}$  -- tries to increase

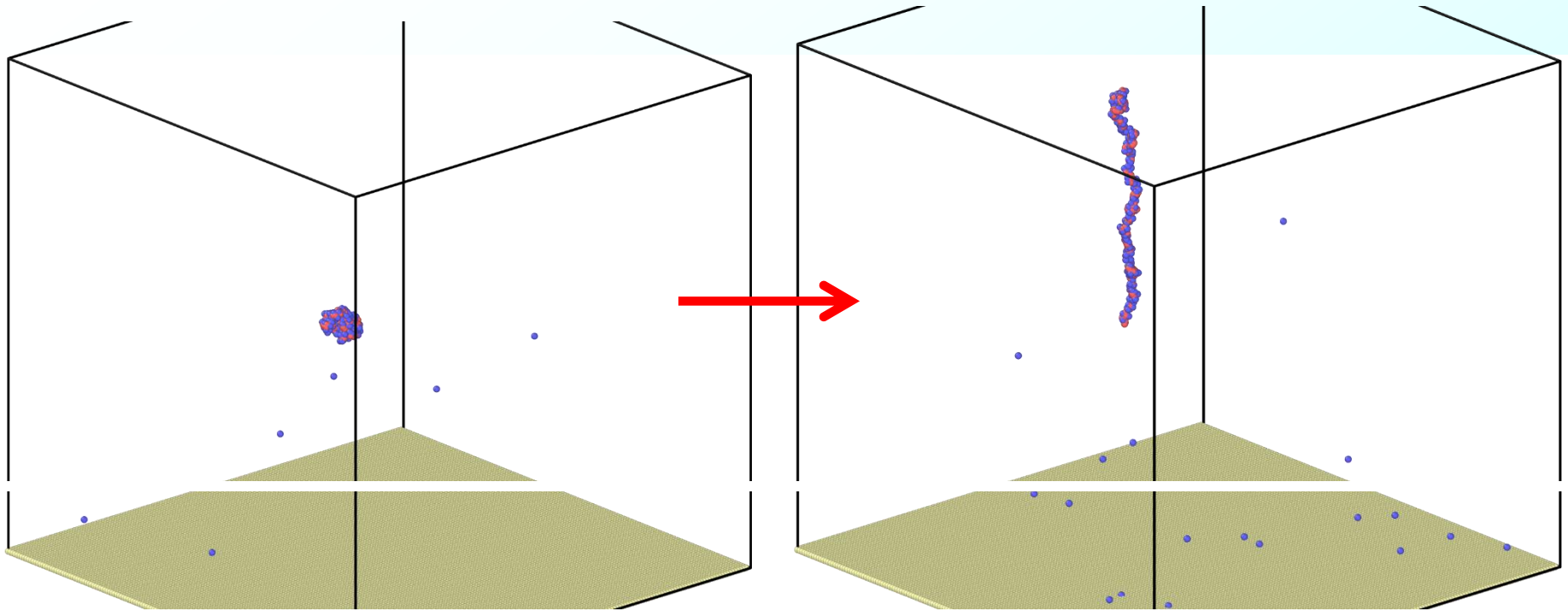


External field term **wins** if:  $\frac{\ell_B}{\alpha N^{\frac{1}{6}}} \ll eEL/k_B T \rightarrow \alpha \gg 1$

$$R_g \sim \ell_B^{1/3} N \quad \text{-- stretched chain}$$

$$E_c \sim \frac{\ell_B^{7/6}}{L} \quad \text{--critical field}$$

Similar setup for **unfixed** chain: R. Netz, PRL 2003

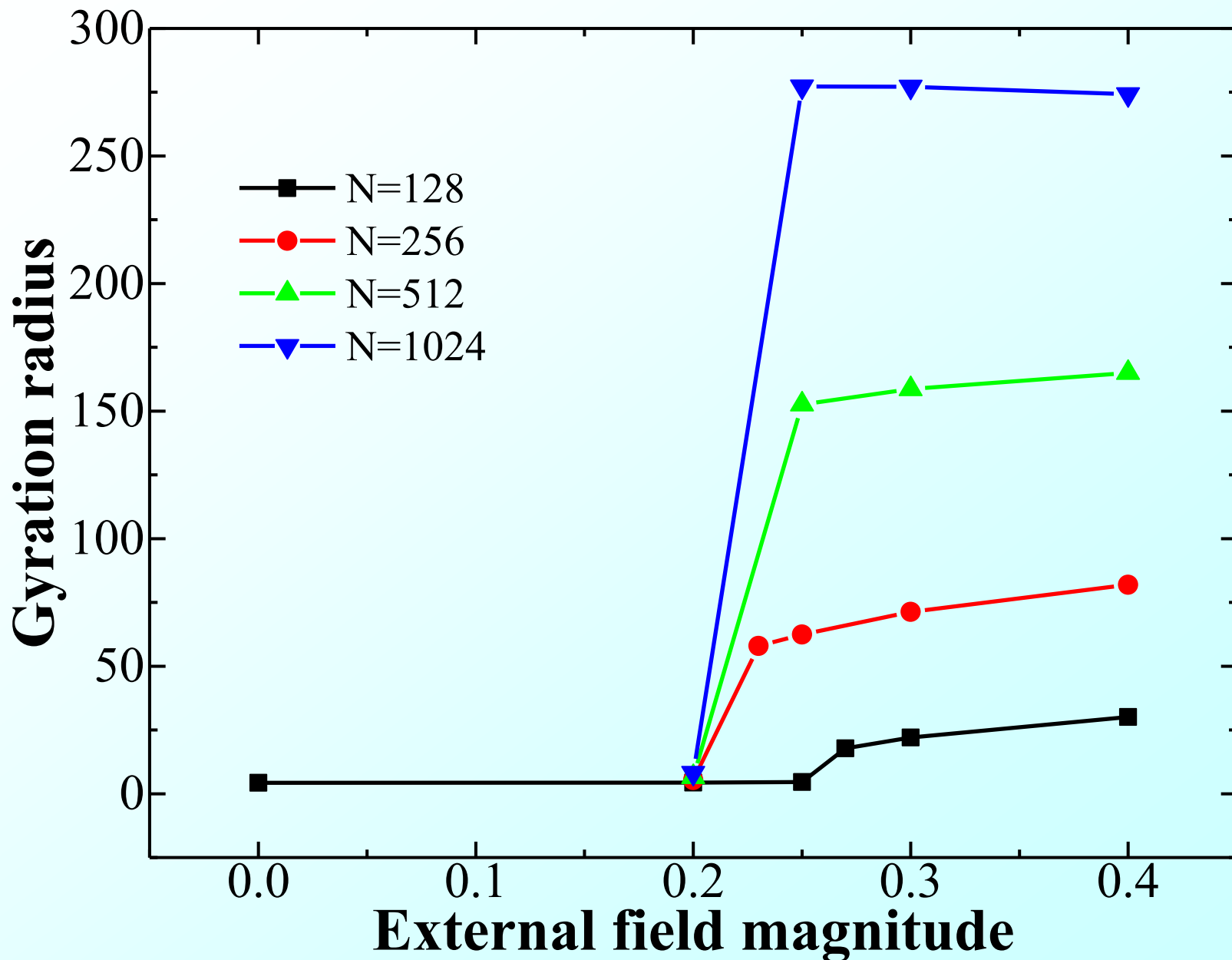


External field term **wins** if:  $\frac{\ell_B}{\alpha N^{1/6}} \ll eEL/k_B T \rightarrow \alpha \gg 1$

$$R_g \sim \ell_B^{1/3} N \quad \text{-- stretched chain}$$

$$E_c \sim \frac{\ell_B^{7/6}}{L} \quad \text{--critical field does not depend on } N$$

# *Simulations: Critical Field is almost size-independent*

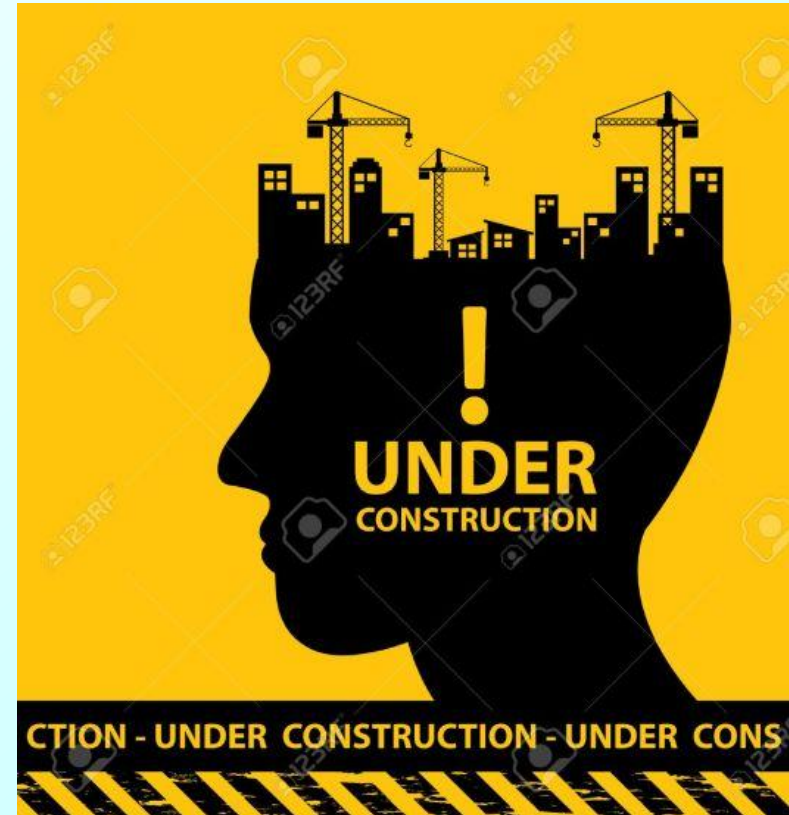
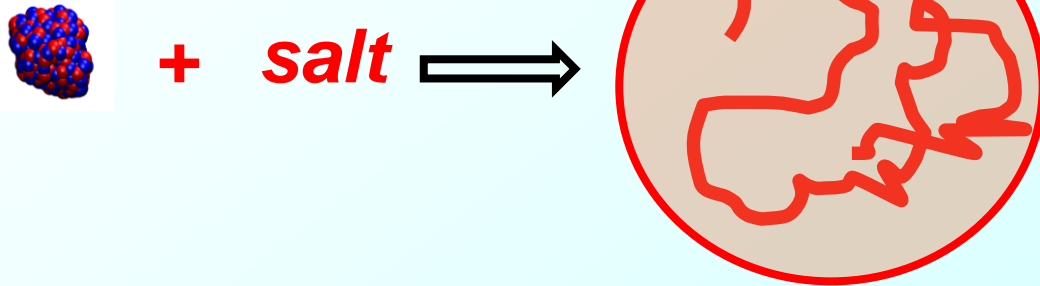


# ***Collapse regulated by added salt***

***With the addition of salt ions the electrostatic component of the free energy will be less important than the entropic and volume component.***

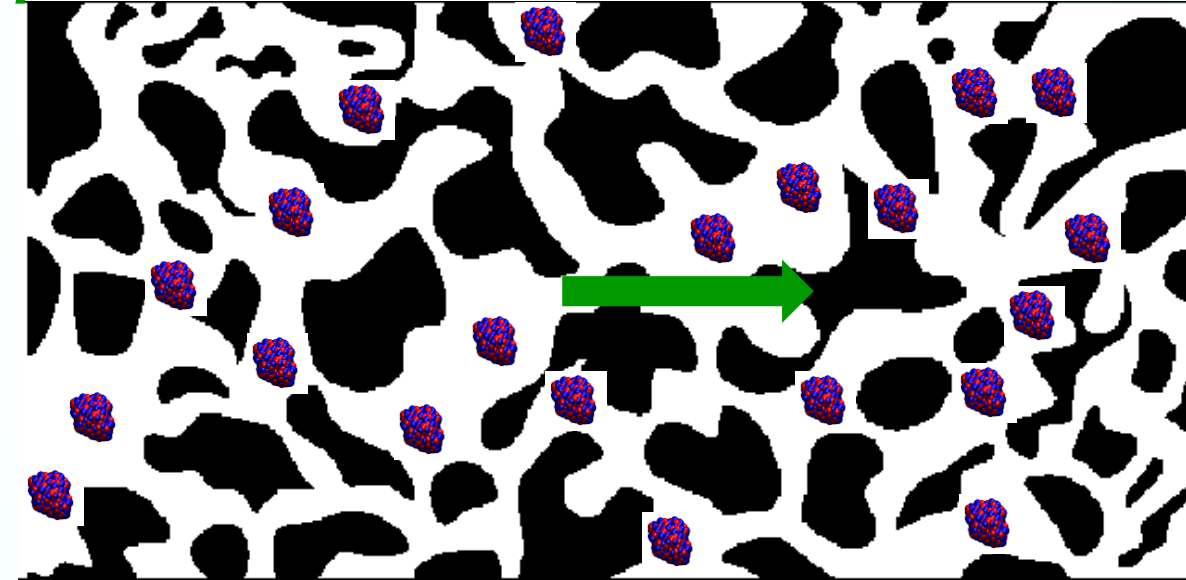
***Hence the common swelling  $R_g \sim N^{0.6}$  is expected.***

***The theory is***

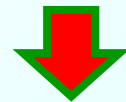


# Possible practical problems

*porous media*



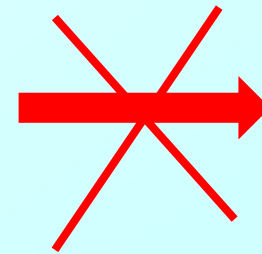
*“Easy Flux” of solvent with polymer*



*added salt*



*Flux is stuck*



## **Conclusion:**

### **Take-home message**

**Electrostatic collapse is driven by *correlated fluctuations of charge density* and *not by* dipole-dipole interactions**

**Two regimes of electrostatic collapse of a polyelectrolyte chain are observed: a *weak electrostatic collapse and strong electrostatic collapse***

**External electric field can *suppress the electrostatic collapse*; in static case the critical field *does not depend* on the chain length.**

***Added salt* can also *suppress the electrostatic collapse*.**

**Controlling *the electrostatic collapse by the characteristics of the solvent* a flux *through porous media* may be regulated**